







**Question 1 continued**

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*(This area contains 28 horizontal lines for writing the answer to Question 1.)*

Q1

**(Total 5 marks)**



N 3 4 2 7 2 A 0 3 2 8

3

**Turn over**



2.

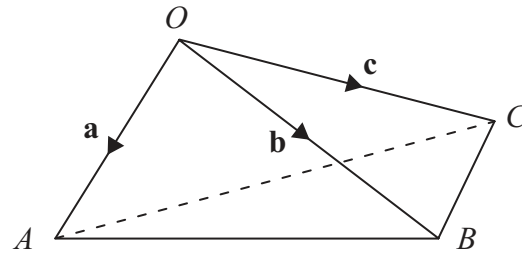


Figure 1

The points  $A$ ,  $B$  and  $C$  have position vectors  $\mathbf{a}$ ,  $\mathbf{b}$  and  $\mathbf{c}$  respectively, relative to a fixed origin  $O$ , as shown in Figure 1.

It is given that

$$\mathbf{a} = \mathbf{i} + \mathbf{j}, \quad \mathbf{b} = 3\mathbf{i} - \mathbf{j} + \mathbf{k} \quad \text{and} \quad \mathbf{c} = 2\mathbf{i} + \mathbf{j} - \mathbf{k}.$$

Calculate

- (a)  $\mathbf{b} \times \mathbf{c}$ , (3)
- (b)  $\mathbf{a} \cdot (\mathbf{b} \times \mathbf{c})$ , (2)
- (c) the area of triangle  $OBC$ , (2)
- (d) the volume of the tetrahedron  $OABC$ . (1)

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**Question 2 continued**

Lined writing area for the question response.

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**Q2**

**(Total 8 marks)**



3.

$$\mathbf{M} = \begin{pmatrix} 6 & 1 & -1 \\ 0 & 7 & 0 \\ 3 & -1 & 2 \end{pmatrix}$$

(a) Show that 7 is an eigenvalue of the matrix  $\mathbf{M}$  and find the other two eigenvalues of  $\mathbf{M}$ . **(5)**

(b) Find an eigenvector corresponding to the eigenvalue 7. **(4)**

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4.

$$\frac{d^2y}{dx^2} + (1+y^2)\frac{dy}{dx} + y = e^{2x}$$

At  $x = 0$ ,  $y = 1$  and  $\frac{dy}{dx} = 2$ .

(a) Find the value of  $\frac{d^3y}{dx^3}$  at  $x = 0$ .

(6)

Given that the value of  $\frac{d^4y}{dx^4}$  at  $x = 0$  is 40,

(b) express  $y$  as a series in ascending powers of  $x$ , up to and including the term in  $x^4$ .

(4)

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Leave blank

**Question 5 continued**

Lined area for writing answers to Question 5.

**Q5**

**(Total 11 marks)**









**Question 6 continued**

Leave  
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Area for writing the answer to Question 6, consisting of multiple horizontal lines.

















**Question 8 continued**

Leave blank

Lined writing area for the answer.



N 3 4 2 7 2 A 0 2 5 2 8





Question 8 continued

Leave blank

Lined writing area for the answer to Question 8.

(Total 11 marks)

Q8

Grading box for Q8

TOTAL FOR PAPER: 75 MARKS

END

